

# Mapping the magneto-structural quantum phases of $\text{Mn}_3\text{O}_4$

M. Kim, X.M. Chen, E. Fradkin, P. Abbamonte, S.L. Cooper  
*Department of Physics and Frederick Seitz Materials Research Laboratory,*  
*University of Illinois, Urbana, Illinois 61801, USA*  
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We present temperature-dependent x-ray diffraction and temperature- and field-dependent Raman scattering studies of single crystal  $\text{Mn}_3\text{O}_4$ , which reveal the novel magnetostructural phases that evolve in the spinels due to the interplay between strong spin-orbital coupling, geometric frustration, and applied magnetic field. We observe a structural transition from tetragonal to monoclinic structures at the commensurate magnetic transition at  $T_2=33\text{K}$ , show that the onset and nature of this structural transition can be controlled with an applied magnetic field, and find evidence for a field-tuned quantum phase transition to a tetragonal incommensurate or spin glass phase.

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Strong coupling among the spin, lattice, and orbital degrees of freedom in the geometrically frustrated spinel compounds [1] results in a rich variety of exotic magnetic and structural phases and properties that are of both scientific and technological interest. For example, the chromium-oxide spinels  $\text{AB}_2\text{O}_4$  ( $A=\text{Zn, Cd, Hg}$ ;  $B=\text{Cr}$ ) exhibit three-dimensional spin-Peierls transitions involving coupled magnetic and structural transitions; [2-6] the vanadium-oxide spinels  $\text{AB}_2\text{O}_4$  ( $A=\text{Zn, Cd, Mn}$ ;  $B=\text{V}$ ) display complex spin/orbital ordering and technologically useful phenomena such as large magnetoelastic and magnetodielectric effects; [7-14] and sulfur-based spinels such as  $\text{FeB}_2\text{S}_4$  ( $B=\text{Cr, Sc}$ ) [15] exhibit orbital-liquid or -glass ground states in which frustration prevents orbital ordering down to  $T=0$ . The rich magnetostructural phases of the spinels are thought to be governed by the interplay between spin-orbital coupling, applied magnetic field, and frustrated exchange interactions, [1,16] but there has been little experimental investigation of the microscopic details of this interplay.

The binary spinel  $\text{Mn}_3\text{O}_4$  is a relatively simple system for experimentally studying the complex interplay between structure, spin-orbital coupling, and magnetic field in the spinels: in spite of its simpler chemical composition—with Mn ions at both tetrahedral ( $A=\text{Mn}^{2+}$ ) and octahedral ( $B=\text{Mn}^{3+}$ ) sites— $\text{Mn}_3\text{O}_4$  exhibits the rich magneto-structural transitions characteristic of more complex ternary magnetic spinels: Below  $T_C=43\text{K}$ , the spins in  $\text{Mn}_3\text{O}_4$  exhibit Yafet-Kittel-type ferrimagnetic ordering, in which the net spin of the octahedrally coordinated  $\text{Mn}^{3+}$  spins is antiparallel to the  $[110]$  direction of the tetrahedrally coordinated  $\text{Mn}^{2+}$  spins, with pairs of  $\text{Mn}^{3+}$  spins canted by  $\pm\theta_{YK}$  from the  $[\bar{1}\bar{1}0]$  direction, where  $\cos\theta_{YK}=0.38$  (0.33) at  $T=4.7\text{K}$  and  $\cos\theta_{YK}=0.40$  (0.25) at  $T=29\text{K}$  for the “non-doubling” octahedral (“doubling” octahedral) site. [14,17] However, below  $T_1=39\text{K}$ ,  $\text{Mn}_3\text{O}_4$  develops an incommensurate sinusoidal or spiral spin structure of the  $\text{Mn}^{3+}$  spins; and below  $T_2=33\text{K}$ ,  $\text{Mn}_3\text{O}_4$  exhibits a commensurate spin structure in which the magnetic unit

cell doubles the chemical unit cell. [17,18] Recent studies also show that the magnetic transitions in  $\text{Mn}_3\text{O}_4$  are associated with significant temperature- and field-dependent changes in the dielectric constant and lattice parameters, reflecting strong spin-lattice coupling in this material. [19,20]

In this paper, we report Raman spectroscopy and x-ray diffraction measurements of the temperature- and magnetic-field-dependent phases of single-crystal  $\text{Mn}_3\text{O}_4$ . These combined measurements offer a particularly clear, microscopic view of the diverse magnetostructural phases that can result from the interplay between strong spin-orbital coupling, geometric frustration, and applied magnetic field in the spinels; this includes evidence for a quantum phase transition to a tetragonal spin/orbital glass phase for intermediate fields with  $H\parallel[\bar{1}\bar{1}0]$ , which we propose is caused by a field-tuned degeneracy between magneto-structural states.

A single-crystal sample of  $\text{Mn}_3\text{O}_4$  was grown at the University of Illinois using a floating zone technique; the sample was identified as a single phase crystal using both x-ray powder diffraction with a Rigaku D-Max system and a pole figure analysis with a Phillips X’pert system. Field-dependent Raman measurements were performed as described previously [21] on an as-grown surface of single crystal  $\text{Mn}_3\text{O}_4$  having a surface normal along the  $[110]$  direction. Temperature-dependent x-ray measurements were carried out using a Rigaku rotaflex RU-300 with a closed-cycle He refrigerator in the range of 10K to 75K. In addition, a Phillips MRD X’Pert was used for high precision measurements at room temperature. Both measurements were performed on the as-grown  $[110]$  surface of single crystal  $\text{Mn}_3\text{O}_4$ . A least squares program was used to determine the lattice parameters of the crystal from the data.

The room-temperature Raman spectrum of our  $\text{Mn}_3\text{O}_4$  sample exhibits 5 phonon peaks, consistent with previous reports: [22] a  $T_{2g}$  symmetry mode at  $290\text{ cm}^{-1}$ , an  $E_g$  symmetry mode at  $320\text{ cm}^{-1}$ ,  $T_{2g}$  symmetry modes at  $375\text{ cm}^{-1}$  and  $479\text{ cm}^{-1}$ , and an  $A_{1g}$  symmetry mode

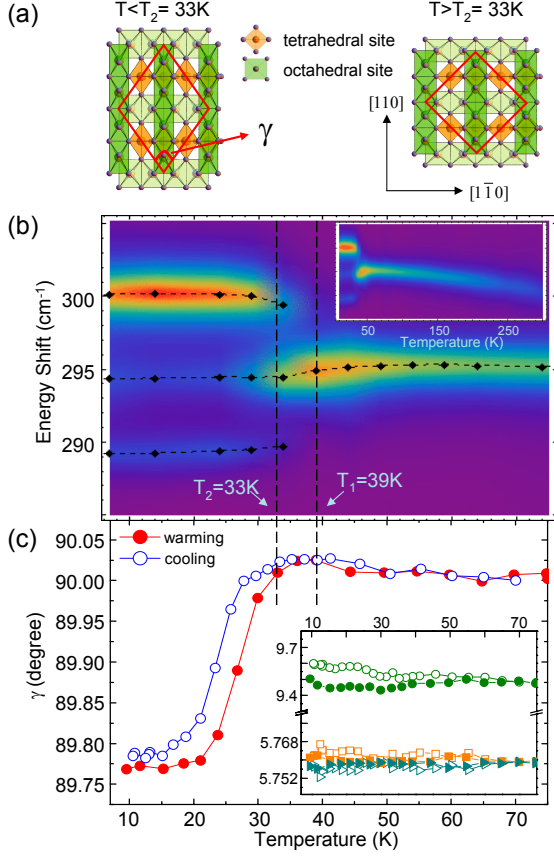


FIG. 1: (a) Illustrations of the monoclinic structure for  $T < T_2 = 33\text{K}$  and the tetragonal structure of  $\text{Mn}_3\text{O}_4$  for  $T > T_2 = 33\text{K}$ . (b) Contour plot of the  $T_{2g}$  phonon mode intensity as functions of energy and increasing temperature, where red=700 counts and blue=0 counts. (inset) Contour plot of the  $T_{2g}$  phonon mode intensity over the full temperature range 7-290K. (c) Temperature dependence of  $\gamma$ —the angle between the  $a$ - and  $b$ -axis directions—as functions of increasing temperature (closed symbols) and decreasing temperature (open symbols). (inset) Temperature dependence [in K] of lattice constants  $a$  (squares),  $b$  (triangles), and  $c$  (circles) [in Å] for  $\text{Mn}_3\text{O}_4$ . Open (closed) symbols represent measurements taken with decreasing (increasing) temperature.

at  $660\text{ cm}^{-1}$ . [22,23] In this paper, we focus on the lowest energy  $T_{2g}$  phonon mode, which is associated with Mn-O bond-stretching vibrations of the tetrahedral site ions. [22,23]

Fig. 1(b) shows the temperature dependence of the  $T_{2g}$  mode intensity and the  $T_{2g}$  mode energy and linewidth for light polarized along the  $[1\bar{1}0]$  crystallographic direction of  $\text{Mn}_3\text{O}_4$ . Three distinct temperature regimes can be identified: (i)  $T > T_1 = 39\text{K}$  – Above  $T_1 = 39\text{K}$ , the  $T_{2g}$  mode narrows and shifts to higher frequencies with decreasing temperature in a conventional manner, i.e., consistent with a temperature dependence governed by anharmonic (multi-phonon) effects. [24] (ii)  $T_2 = 33\text{K} < T \leq T_1 = 39\text{K}$  – In the incommensurate magnetic phase regime between  $T_2 = 33\text{K}$  and  $T_1 = 39\text{K}$ , the lowest  $T_{2g}$  mode decreases in energy slightly with decreasing tem-

perature due to magnetoelastic effects, but exhibits no evidence for a change in structural symmetry. (iii)  $T < T_2 = 33\text{K}$  – Below the commensurate magnetic transition  $T_2 = 33\text{K}$ , the  $T_{2g}$  mode abruptly splits into three modes near  $290\text{ cm}^{-1}$ ,  $295\text{ cm}^{-1}$ , and  $300\text{ cm}^{-1}$ . This splitting is consistent with a tetragonal-to-monoclinic distortion below  $T_2$ , which splits the degenerate  $T_{2g}$  mode by expanding the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the easy-axis  $[110]$  direction and contracting the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the hard-axis  $[1\bar{1}0]$  direction (see illustrations, Fig. 1(a)). Note that the relative intensities of the three modes shown in Fig. 1(b) for  $T < T_2$  confirm that the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length expands along the easy-axis  $[110]$  direction below  $T_2 = 33\text{K}$ : the higher-energy ( $\sim 300\text{ cm}^{-1}$ ) split mode—which is associated with vibrations of the contracted  $\text{Mn}^{2+}\text{-O}^{2-}$  bond—exhibits the strongest light scattering intensity, indicating that the contracted  $\text{Mn}^{2+}\text{-O}^{2-}$  bond is oriented in the direction of the incident light polarization, i.e., along the  $[1\bar{1}0]$  direction. By contrast, the intensity of the lower-energy ( $\sim 290\text{ cm}^{-1}$ ) split mode—which is associated with vibrations of the expanded  $\text{Mn}^{2+}\text{-O}^{2-}$  bond—has a substantially weaker intensity than the  $\sim 300\text{ cm}^{-1}$  mode, consistent with an expansion of the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond in a direction perpendicular to the incident light polarization, i.e., along the  $[110]$  direction.

To provide more definitive evidence for a tetragonal-to-monoclinic phase transition below  $T_2$  in  $\text{Mn}_3\text{O}_4$ , temperature-dependent x-ray diffraction measurements were performed on the same crystal. Fig. 1(c) shows the temperature dependence of the lattice parameters  $a$ ,  $b$ ,  $c$ , and  $\gamma$ —the angle between  $a$  and  $b$ —as functions of both increasing (“warming”) and decreasing (“cooling”) temperature. While  $\gamma$  exhibits an abrupt decrease near  $T_2 = 33\text{K}$ —indicating an abrupt decrease in the angle between  $a$ - and  $b$ -axis directions at this temperature, the lattice parameters  $a$  and  $b$  exhibit no significant temperature dependence, and the lattice parameter  $c$  exhibits only a weak temperature dependence and hysteretic behavior. This behavior confirms that  $\text{Mn}_3\text{O}_4$  exhibits a first-order tetragonal-to-monoclinic structural phase transition near  $T_2 = 33\text{K}$ , as illustrated schematically in Fig. 1(a). Notably, the observed monoclinic crystal structure we observe below  $T_2 = 33\text{K}$  is consistent with the spin structure that has been previously reported for  $\text{Mn}_3\text{O}_4$  below  $T_2$ : the coplanar spin structure of the doubled unit cell has spins lying within the  $(1\bar{1}0)$  plane with a net spin along  $[110]$ , in which the  $\text{Mn}^{3+}$  spins are canted by an angle  $\pm\theta_{YK}$  from the  $[\bar{1}\bar{1}0]$  direction. This spin canting is associated with a tilting of the  $d_{3z^2-r^2}$  orbitals of  $\text{Mn}^{3+}$  toward the  $[\bar{1}\bar{1}0]$  direction due to spin-orbital coupling, which results in a tilting of  $\text{Mn}^{3+}$  octahedra and an expansion of the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the  $[110]$  direction. [17,20] We also note that the tetragonal structure we observe for the incommensurate magnetic phase regime between  $T_2 = 33\text{K}$  and  $T_1 = 39\text{K}$

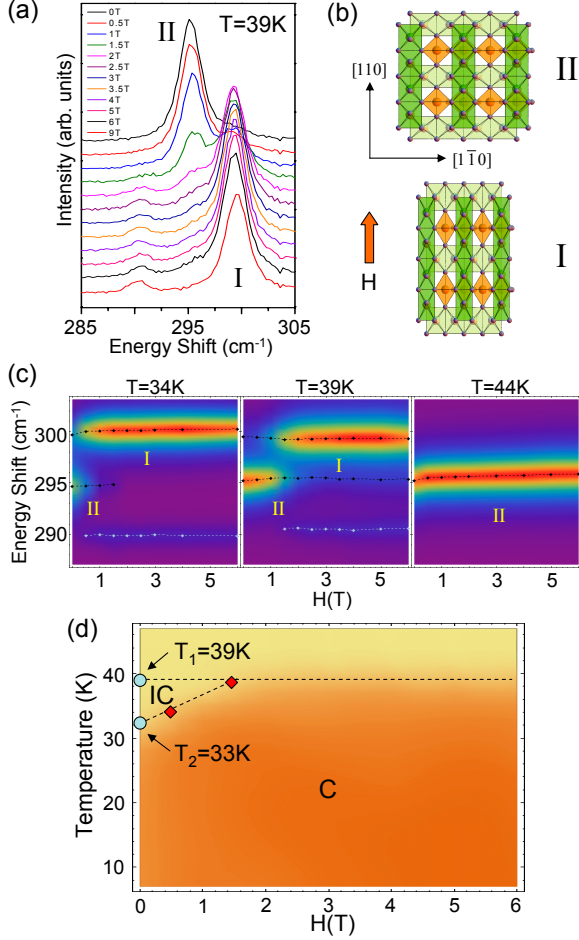


FIG. 2: (a) Field dependence of the Raman spectra at  $T=39\text{K}$  for  $H\parallel[110]$ . (b) Illustrations of the  $\text{Mn}_3\text{O}_4$  structure in (top) the low-field undistorted phase and (bottom) the high-field monoclinic phase. (c) Contour plots of the intensities of the split modes as functions of energy and field at (left)  $T=34\text{K}$ , (middle)  $39\text{K}$ , and (right)  $44\text{K}$ , where red=700 counts and blue=0 counts for  $H\parallel[110]$ . (d) Phase diagram as functions of magnetic field (along  $[110]$ ) and temperature; orange region=structure I, yellow region=structure II, IC=incommensurate magnetic phase, C=commensurate (cell-doubled) magnetic phase.

(Fig. 1(b)) is consistent with the presence of an axially symmetric spiral spin structure [17] in this temperature regime.

The distinctive Raman spectroscopic signatures associated with the different magneto-structural phases in  $\text{Mn}_3\text{O}_4$ —illustrated in Fig. 1(b)—offer a convenient method for investigating the phases induced with an applied magnetic field. Fig. 2 illustrates the field-induced structural phases of  $\text{Mn}_3\text{O}_4$  for fields applied along the easy-axis  $[110]$  direction. Fig. 2(a) and the left and middle plots of Fig. 2(c) show that, in the incommensurate magnetic phase regime  $T_2=33\text{K} < T \leq T_1=39\text{K}$ , the  $\sim 295\text{cm}^{-1}$  mode associated with the undistorted tetragonal phase (structure II in Fig. 2(b)) exhibits a field-induced splitting similar to that induced upon cooling

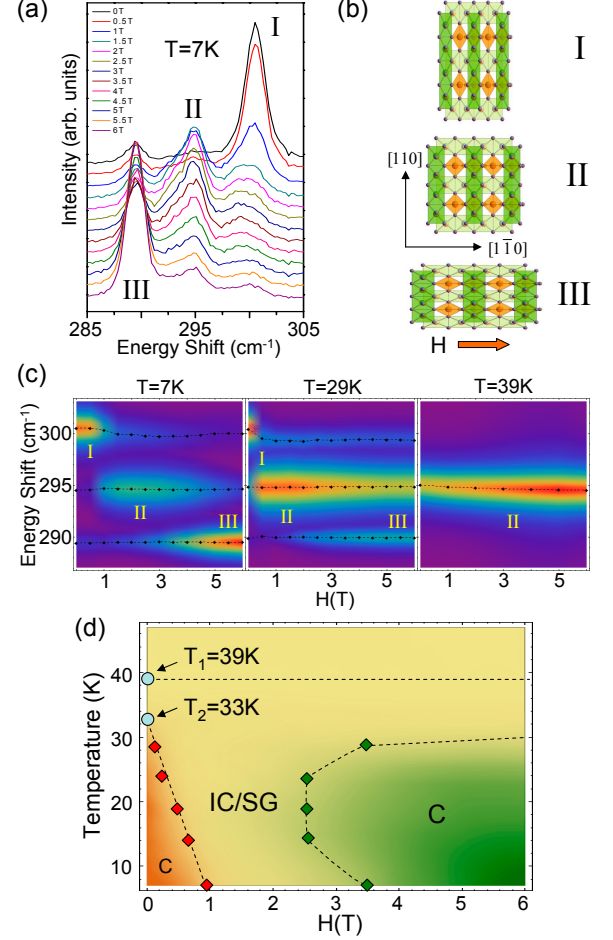


FIG. 3: (a) Field dependence of the Raman spectra at  $T=7\text{K}$  for a magnetic field applied along the hard-axis  $[1\bar{1}0]$  direction. (b) Illustrations of the  $\text{Mn}_3\text{O}_4$  structure in (top) the low-field monoclinic phase, (middle) the intermediate undistorted tetragonal phase, and (bottom) the high-field monoclinic phase. (c) Contour plots of the intensities of the split modes as functions of energy and field at (left)  $T=7\text{K}$ , (middle)  $29\text{K}$ , and (right)  $39\text{K}$ , where red=700 counts and blue=0 counts for  $H\parallel[1\bar{1}0]$ . (d) Phase diagram as functions of magnetic field (along  $[1\bar{1}0]$ ) and temperature; orange region=structure I, yellow region=structure II, green region=structure III, IC/SG=incommensurate or spin glass magnetic phase, and C=commensurate (cell-doubled) magnetic phase.

below  $T_2=33\text{K}$  in zero magnetic field (Fig. 1(b)). Thus, in the incommensurate magnetic phase, an applied magnetic field along the easy axis  $[110]$  direction induces a tetragonal-to-monoclinic distortion in  $\text{Mn}_3\text{O}_4$  by forcing the  $\text{Mn}^{3+}$  spins to order within the  $(1\bar{1}0)$  plane and inducing the cell-doubled coplanar magnetic structure associated with the monoclinic structure (see Fig. 2(b)). This strong magnetoelastic response at rather modest fields likely arises from a field-induced increase—via spin-orbit coupling—in the hybridization between the  $d_{3z^2-r^2}$  and  $d_{xy}$  orbitals of  $\text{Mn}^{3+}$  for  $H\parallel[110]$ , and demonstrates that the magnetostructural states I and II in Fig. 2(b) have

very similar free energies. Fig. 2(d) summarizes the different magnetic/structural phases of  $\text{Mn}_3\text{O}_4$  as functions of magnetic field and temperature for  $\text{H}||[110]$ .

A richer magneto-structural phase diagram is observed when the magnetic field is applied along the hard-axis  $[1\bar{1}0]$  direction of  $\text{Mn}_3\text{O}_4$ , as illustrated in Fig. 3. Figs. 3(a) and 3(c) show that three different phase regimes are apparent for  $\text{H}||[1\bar{1}0]$  at  $T=7$  K. For  $H < 1$  T, the high-energy  $300\text{cm}^{-1}$  mode is the dominant mode, indicating that the monoclinic distortion with an expanded  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the easy-axis  $[110]$  direction (structure I) persists at low fields. On the other hand, at high magnetic fields, i.e., for  $H > 4$  T for  $T=7$  K, Figs. 3(a) and (c) show that the low-energy  $290\text{cm}^{-1}$  mode is most intense, indicating a monoclinic phase in which the field reorients the Mn spin—and expands the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond lengths—along the hard-axis  $[1\bar{1}0]$  direction (structure III).

Most remarkably, however, Figs. 3(a) and 3(c) show that the field-induced transition from a monoclinic distortion with  $\text{M}||[110]$  to a monoclinic distortion with  $\text{M}||[1\bar{1}0]$  is not abrupt, but occurs via an intermediate field regime ( $1\text{ T} < H < 4\text{ T}$ ) in which the dominant mode is the  $\sim 295\text{cm}^{-1}$  mode, i.e., the mode associated with the undistorted tetragonal phase (structure II in Figs. 3(b) and 3(c)) observed in the paramagnetic and incommensurate phases above  $T_2=33\text{ K}$  for  $H=0$  (Fig. 1(b)). We suggest that the quantum phase transition to this intermediate phase is a transition from a ferrimagnetic, monoclinic phase with  $\text{M}||[110]$ , to a “spin/orbital” glass phase—in which the Mn spins are randomly oriented along the  $[110]$  and  $[1\bar{1}0]$  directions—or to an incommensurate spiral spin phase; both of these possibilities are consistent with a tetragonal structure (see Fig. 1(b)). Fig. 3(c) shows that, with increasing temperatures, this field-induced tetragonal regime becomes more pronounced. Fig. 3(d) summarizes the different magnetic/structural phases of  $\text{Mn}_3\text{O}_4$  as functions of magnetic field and temperature for  $\text{H}||[1\bar{1}0]$ .

The results summarized in Fig. 3(d) indicate that the competition between spin-orbital coupling, geometrical frustration, and applied magnetic field in  $\text{Mn}_3\text{O}_4$  leads to an incommensurate—or even glassy—spin state at  $T=0$  that is sandwiched—as a function of applied field with  $\text{H}||[1\bar{1}0]$ —between commensurate spin phases. The observation of a quantum phase transition to an intermediate incommensurate or spin-glass tetragonal phase (structure II in Fig. 3(b))—rather than a simple metamagnetic transition between or coexistence of commensurate ferrimagnetic phases (structures I and III in Fig. 3(b)) at intermediate fields—likely reflects the importance of spin-lattice coupling in  $\text{Mn}_3\text{O}_4$ , wherein the balancing of elastic and magnetic energies favors the formation of a more isotropic magnetostructural configuration at intermediate fields with  $\text{H}||[1\bar{1}0]$ . Indeed, this more isotropic magnetostructural configuration (II) appears to

be the means by which  $\text{Mn}_3\text{O}_4$  resolves the frustration that arises from the field-induced degeneracy between  $\text{M}||[110]$  and  $\text{M}||[1\bar{1}0]$  spin configurations at intermediate field values with  $\text{H}||[1\bar{1}0]$ . Field-dependent neutron scattering and heat capacity measurements would be useful for clarifying the nature of the spin configuration and entropy of this highly frustrated field-induced state. It is also important to study the  $T\sim 0$  spin dynamics of this intermediate-field isotropic phase, in particular to explore the extent to which quantum critical fluctuations govern the dynamics in this frustrated phase regime.

In summary, combined temperature- and field-dependent Raman scattering and temperature-dependent x-ray scattering studies provide a clear microscopic view of the diverse and complex magnetostructural phases that evolve in the spinel material  $\text{Mn}_3\text{O}_4$  due to the interplay between spin-orbital coupling, geometrical frustration, and applied magnetic field. In addition to identifying the specific structural phases associated with the different magnetic states observed in  $\text{Mn}_3\text{O}_4$  with  $H=0$ , we have identified the microscopic magnetostructural changes that are associated with the novel magnetodielectric behavior previously observed for this material. Most interesting is the observation of a quantum phase transition to a structurally isotropic, incommensurate/disordered spin state for intermediate fields with  $\text{H}||[1\bar{1}0]$ , which reflects a compromise this system takes to accommodate the frustration imposed by a field-induced degeneracy between differing magnetostructural states.

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